

## AS-84.3127 Paikannus- ja navigointimenetelmät

### Laskuharjoitus 3.

1.

Tunnetaan kahden puun xy-koordinaatit:

$$x_1 = -1 \text{ m ja } y_1 = 10 \text{ m}$$

$$x_2 = 1 \text{ m ja } y_2 = 10 \text{ m}$$

Robotti mittaa laserilla etäisyyden  $d$  molempiin puihin

$$d_1 = 10.05 \text{ m ja } d_2 = 10.05 \text{ m}$$

Mikä on robotin paikka?

Jos mittaus  $d_2$  on -10 cm virheellinen, eli  $d_2 = 9.95 \text{ m}$ , niin kuinka iso virhe syntyy x-suunnassa ja y-suunnassa.

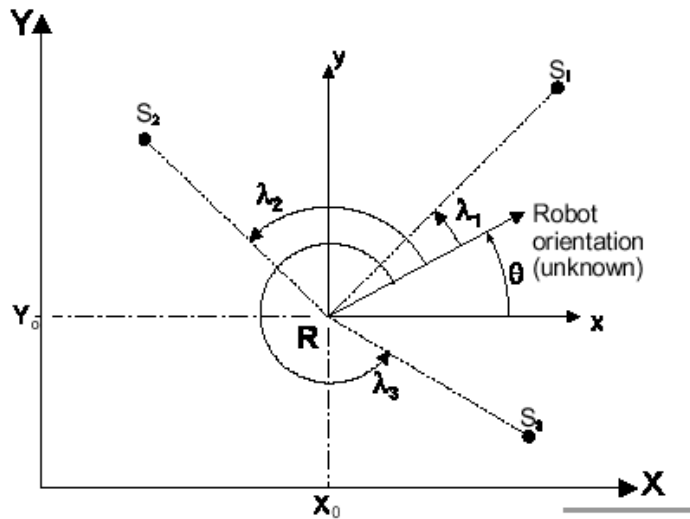
Eli laske  $x_{dop}$  ja  $y_{dop}$

$$\Delta x = x_{dop} \cdot \Delta d$$

$$\Delta y = y_{dop} \cdot \Delta d$$

2.

Laske robotin paikka ja asento kulmamittausperiaatetta (triangulation) käyttäen kuvan kaltaisessa tapauksessa.



**Figure 6.1:** The basic triangulation problem: a rotating sensor head measures the three angles  $\lambda_1$ ,  $\lambda_2$ , and  $\lambda_3$  between the vehicle's longitudinal axes and the three sources  $S_1$ ,  $S_2$ , and  $S_3$ .

Majakoiden koordinaatit ovat  $S_1(x=5,y=5)$ ,  $S_2(0,5)$  ja  $S_3(5,0)$ . Kulmamittausarvot ovat  $\lambda_1=0$ ,  $\lambda_2=90$  ja  $\lambda_3=270$  astetta.

## AS-84.3127 Localization- and navigation methods

### Exercise 3.

#### 1.

The xy-coordinates of two trees are known:

$$x_1 = -1 \text{ m and } y_1 = 10 \text{ m}$$

$$x_2 = 1 \text{ m and } y_2 = 10 \text{ m}$$

The robot measures the distance  $d$  to both trees with a laser

$$d_1 = 10.05 \text{ m and } d_2 = 10.05 \text{ m}$$

What is the position of the robot?

If measurement  $d_2$  has an error  $-10$  cm, that is  $d_2 = 9.95$  m, then how large is the resulting position error in x- and y-direction.

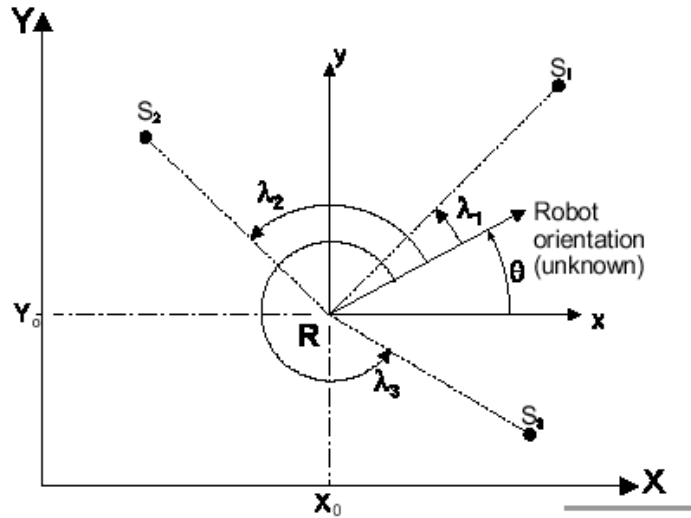
in other words, calculate  $x_{dop}$  and  $y_{dop}$

$$\Delta x = x_{dop} * \Delta d$$

$$\Delta y = y_{dop} * \Delta d$$

2.

Calculate the robots position and heading in a situation such as depicted in the figure below, using triangulation.



**Figure 6.1:** The basic triangulation problem: a rotating sensor head measures the three angles  $\lambda_1$ ,  $\lambda_2$ , and  $\lambda_3$  between the vehicle's longitudinal axes and the three sources  $S_1$ ,  $S_2$ , and  $S_3$ .

The beacon coordinates are  $S_1(x=5,y=5)$ ,  $S_2(0,5)$  and  $S_3(5,0)$ . Bearing measurements are  $\lambda_1=0$ ,  $\lambda_2=90$  ja  $\lambda_3=270$  degrees.